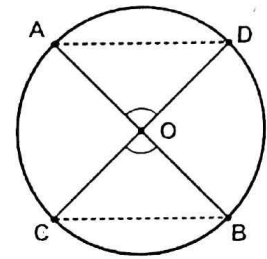


## EXERCISE 11.1

**Q.1** In a circle two equal diameters  $\overline{AB}$  and  $\overline{CD}$  intersect each other. Prove that  $m\widehat{AD} = m\widehat{BC}$ .

**Given:** A circle with centre "O". Two diameters  $\overline{AB}$  and  $\overline{CD}$ , intersecting at point O.



**To Prove:**  $m\widehat{AD} = m\widehat{BC}$

**Construction:**

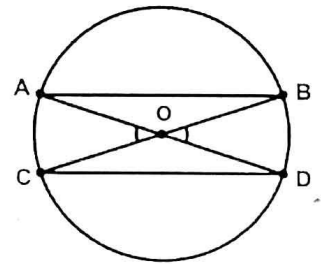
Join A to D and C to B

**Proof:**

Statements	Reasons
In $\triangle AOD \leftrightarrow \triangle BOC$	
$\overline{OA} \cong \overline{OB}$	Radii of the same circle
$\angle AOD \cong \angle BOC$	Vertical angles are congruent
$\overline{OD} \cong \overline{OC}$	Radii of the same circle
$\therefore \triangle AOD \cong \triangle BOC$	S. A. S $\cong$ S. A. S
$\overline{AD} \cong \overline{BC}$	Corresponding sides of congruent triangle
Or $m\widehat{AD} = m\widehat{BC}$	

**Q.2.** In a circle prove that the arcs between two parallel and equal chords are equal.

**Given:** A circle with centre O. Two chords  $\overline{AB}$  and  $\overline{CD}$  Such that  $\overline{AB} \parallel \overline{CD}$  and  $m\widehat{AB} = m\widehat{CD}$



**To Prove:**  $m\widehat{AC} = m\widehat{BD}$

**Construction:** Join A to D and B to C. Such that  $\overline{AD}$  and  $\overline{BC}$  intersect each other at central point O.

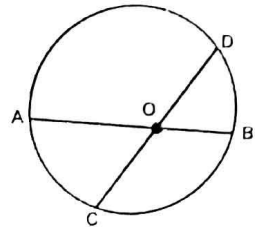
**Proof:**

Statements	Reasons
$\overline{AD}$ and $\overline{BC}$ are line segment intersecting at centre O.	
$\angle AOC$ and $\angle BOD$ are central angles.	Angle subtended at centre.
$m\angle AOC = m\angle BOD$	Vertical angles
$m\widehat{AC} = m\widehat{BD}$	Within the same circle arcs opposite to the equal central angles are equal.

**Q.3. Give a geometric proof that a pair of bisecting chords are the diameters of a circle.**

**Given:** A circle and two chords  $\overline{AB}$  and  $\overline{CD}$  bisecting each other at point O. i.e.

$$m\overline{AO} = m\overline{OB} \text{ and } m\overline{CO} = m\overline{OD}$$



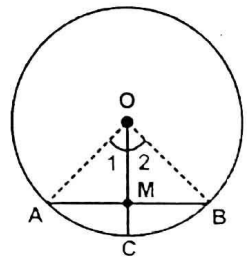
**To Prove:** Chords  $\overline{AB}$  and  $\overline{CD}$  are diameters.

**Proof:**

Statements	Reasons
$m\overline{AB} = m\overline{CD}$ .....(i)	Two chords can bisect each other only when they are equal (given)
$\therefore$ O is the mid point of $\overline{AB}$ and $\overline{CD}$	Given
$m\overline{AO} = m\overline{BO} = \frac{1}{2} m\overline{AB}$ .....(ii)	
$m\overline{DO} = m\overline{CO} = \frac{1}{2} m\overline{CD}$ .....(iii)	
$m\overline{AO} = m\overline{BO} = m\overline{CO} = m\overline{DO}$ .....(iv)	From (i), (ii) and (iii)
The points of circle A, B, C and D are equidistant from the fixed point "O".	From (iv)
This fixed point O is the centre of the circle having the points A, B, C and D.	By definition
As chords $\overline{AB}$ and $\overline{CD}$ pass through the centre "O" therefore chords $\overline{AB}$ and $\overline{CD}$ are diameters.	

**Q.4. If C is the midpoint of an arc ACB in a circle with centre O. Show that line segment OC bisects the chord AB.**

**Given:** A circle with centre "O"  $\widehat{ACB}$  is an arc with C as its midpoint and  $m\widehat{AC} = m\widehat{CB}$ . Center "O" is joined with C such that  $\overline{OC}$  meets  $\overline{AB}$  at M.



**To Prove:**  $m\overline{AM} = m\overline{BM}$

**Construction:** Join center "O" with A and B to make central angle AOB.

**Proof:**

Statements	Reasons
$\angle AOB$ is central angle	Construction
$\therefore m\angle 1 = m\angle 2$ .....(i)	C is the midpoint of $\widehat{ACB}$ (Given)
In $\triangle AOM \longleftrightarrow \triangle BOM$	Common
$\overline{OM} \cong \overline{OM}$	Proved
$\angle 1 \cong \angle 2$	
$\overline{OA} \cong \overline{OB}$	Radii of the same Circle
$\triangle AOM \cong \triangle BOM$	S.A.S $\cong$ S.A.S
$\overline{AM} \cong \overline{BM}$	Corresponding sides of congruent triangles.
Hence $m\overline{AM} = m\overline{BM}$	