

64	Prove that $\frac{\cos 8^\circ - \sin 8^\circ}{\cos 8^\circ + \sin 8^\circ} = \tan 37^\circ$
65	Prove that $\cos 2\theta = \frac{1 - \tan^2 \theta}{1 + \tan^2 \theta}$
66	Show that $\frac{\sin \alpha - \sin \beta}{\sin \alpha + \sin \beta} = \tan \left(\frac{\alpha - \beta}{2} \right) \cot \left(\frac{\alpha + \beta}{2} \right)$
67	Show that $\frac{\cos(90^\circ + \theta) \operatorname{Sec}(-\theta) \tan(180^\circ - \theta)}{\cos 90^\circ} = \tan \theta$
68	Find the measure of the greatest angle, if sides of triangle are 6, 20, 33
69	The measures of side of a triangular plot are 413, 212 & 375 meters. Find the measure of the corner angles of the plot.
70	Prove that $(r_1 + r_2) \tan \frac{\gamma}{2} = a$
71	Prove that $(r_3 + r) \cot \frac{\gamma}{2} = a/3$. Prove that $abc(\sin \alpha + \sin \beta + \sin \gamma) = 4\Delta s$
72	Solve $4\cos^2 x - 3 = 0$
73	Solve the trigonometric equation $\sec^2 \theta = \frac{4}{3}$
74	Verify $\sin^2 \frac{\pi}{6} : \sin^2 \frac{\pi}{4} : \sin^2 \frac{\pi}{3} : \sin^2 \frac{\pi}{2} = 1 : 2 : 3 : 4$
75	Find x , if $\tan^2 45^\circ - \cos^2 60^\circ = x \sin 45^\circ \cos 45^\circ \tan 60^\circ$
76	Verify $\sin^2 \frac{\pi}{6} + \sin^2 \frac{\pi}{4} + \tan^2 \frac{\pi}{4} = 2$
77	Prove that $\sec^2 A + \operatorname{cosec}^2 A = \sec^2 A \operatorname{cosec}^2 A$
78	Show that $\tan^{-1} A + \cot^{-1} A = \frac{\pi}{2}$
79	Prove that $\frac{\tan \frac{\theta}{2} + \cot \frac{\theta}{2}}{\cot \frac{\theta}{2} - \tan \frac{\theta}{2}} = \sec \theta$
80	Prove that $\frac{\operatorname{cosec} \theta + 2 \operatorname{cosec} 2\theta}{\sec \theta} = \cot \frac{\theta}{2}$
81	Prove that $\frac{2 \tan \theta}{1 - \tan^2 \theta} = 2 \sin \theta \cos \theta$
82	Prove that $2 \tan^{-1} A = \tan^{-1} \frac{2A}{1 - A^2}$
83	Prove that $\cos^2 \theta - \sin^2 \theta = \frac{1 - \tan^2 \theta}{1 + \tan^2 \theta}$
84	Prove that $\tan^{-1} A - \tan^{-1} B = \tan^{-1} \frac{A - B}{1 - AB}$
85	Give the range and domain of $\cos^{-1} x$
86	Prove that $\tan^{-1} \frac{120}{119} = 2 \cos^{-1} \frac{12}{13}$
87	Show that $\sin(2 \cos^{-1} x) = 2x\sqrt{1 - x^2}$
88	Prove that $\cos 2\alpha = 2 \cos^2 \alpha - 1$
89	Write the Triple Angle Identity of $\tan 3\alpha$
90	Prove that $\sec \theta \operatorname{cosec} \theta \sin \theta \cos \theta = 1$
91	What is the relation between a radian and a degree?
92	Is the relation $l = r\theta^\circ$ valid?
93	Convert $\frac{19\pi}{32}$ into sexagesimal system.
94	What is the Circular Measure of the angle between hands of a watch at 80' clock?
95	A horse is tethered to a peg by a rope of 9 meters length & it can move in a circle with the peg as center. If the horse moves along the circumference of the circle, keeping the rope tight, how far will it have gone when the rope has turned an angle of 55° ?
96	Define Co-terminal Angles
97	Define Allied Angles
98	$\frac{1 + \cos \theta}{1 - \cos \theta} = (\operatorname{cosec} \theta + \cot \theta)^2$

LONG QUESTIONS

Chapter 2:

Q.1 Prove that $p \vee (\sim p \wedge \sim q) \vee (p \wedge q) = p \vee (\sim p \wedge \sim q)$

Q.2 Convert $(A \cup B) \cup C = A \cup (B \cup C)$ into logical form and prove it by constructing the truth table.

Q.3 Give the logical proof of De Morgan's Law.

Q.4 Convert the theorem $(A \cup B)' = A' \cap B'$ to logical statement and prove them by constructing truth tables.

Q.5 Show that the set $\{1, \omega, \omega^2\}$, $\omega^3 = 1$, is an Abelian group w.r.t ordinary multiplication.

Q.6 Prove that 2×2 non singular matrices over the real field form a non-abelian group under multiplication

Q.7 Consider the set $S = \{1, -1, i, -i\}$. Set up its multiplication table and show that the set S is an abelian group under multiplication.

Q.8 Give logical proofs of the following theorems

i) $A \cap (B \cup C) = (A \cap B) \cup (A \cap C)$

ii) $(A \cup B)' = A' \cap B'$

Q.9 If a, b are elements of a group G, solve the following equation :

ii) $xa = b$

i) $ax = b$

Chapter 3:

Q.1 Find x and y if $\begin{bmatrix} 2 & x \\ -1 & y \end{bmatrix} + 2 \begin{bmatrix} 1 & x & y \\ 0 & 2 & -1 \end{bmatrix} = \begin{bmatrix} 4 & -2 & 3 \\ 1 & 6 & 1 \end{bmatrix}$

Q.2 Solve the following system of linear equations: $3x - 5y = 1$; $-2x + y = -3$

Q.3 Solve the following matrix equation for A: $\begin{bmatrix} 4 & 3 \\ 2 & 2 \end{bmatrix} A - \begin{bmatrix} 2 & 3 \\ -1 & -2 \end{bmatrix} = \begin{bmatrix} -1 & -4 \\ 3 & 6 \end{bmatrix}$ Q.4 Show that $\begin{vmatrix} -a & 0 & c \\ 0 & a & -b \\ b & -c & 0 \end{vmatrix} = 0$

Q.5 Show that $\begin{vmatrix} a + \lambda & b & c \\ a & b + \lambda & c \\ a & b & c + \lambda \end{vmatrix} = \lambda^2(a + b + c + \lambda)$

Q.6 If $A = \begin{bmatrix} 1 & 0 & 2 \\ 0 & 2 & 1 \\ 1 & -1 & 1 \end{bmatrix}$ then find A^{-1} by using adjoint of the matrix.

Q.7 Show that $\begin{vmatrix} x & 1 & 1 & 1 \\ 1 & x & 1 & 1 \\ 1 & 1 & x & 1 \\ 1 & 1 & 1 & x \end{vmatrix} = (x + 3)(x - 1)^3$

Q.8 Show that $\begin{vmatrix} b + c & a & a^2 \\ c + a & b & b^2 \\ a + b & c & c^2 \end{vmatrix} = (a + b + c)(a - b)(b - c)(c - a)$

Q.9 Without expansion, verify that $\begin{vmatrix} 1 & a^2 & \frac{a}{bc} \\ 1 & b^2 & \frac{b}{ca} \\ 1 & c^2 & \frac{c}{ab} \end{vmatrix} = 0$

Q.10 Solve the following systems of linear equations by Cramer's rule.

$$\begin{aligned} 2x + 2y + z &= 3 \\ 3x - 2y - 2z &= 1 \\ 5x + y - 3z &= 2 \end{aligned}$$

Q.11 Use matrices to solve the following systems:

$$\begin{aligned} x - 2y + z &= -1 \\ 3x + y - 2y &= 4 \\ y - z &= 1 \end{aligned}$$

Q.12 Solve the system of linear equations by Cramer's rule.

$$\begin{aligned} 3x_1 - x_2 - x_3 &= -4 \\ x_1 + x_2 - 2x_3 &= -1 \\ -x_1 + 2x_2 - x_3 &= 1 \end{aligned}$$

Q.13 Use matrices to solve the system

$$\begin{aligned} x_1 - 2x_2 + x_3 &= -4 \\ 2x_1 - 3x_2 + 2x_3 &= -6 \\ 2x_1 + 2x_2 + x_3 &= 5 \end{aligned}$$

Chapter 4:

Q.1 Solve by factorization $\frac{a}{ax-1} + \frac{b}{bx-1} = a + b$; $x \neq \frac{1}{a}, \frac{1}{b}$

Q.2 Solve by quadratic formula $(a + b)x^2 + (a + 2b + c)x + b + c = 0$

Q.3 Solve by quadratic formula $(x - a)(x - b) + (x - b)(x - c) + (x - c)(x - a) = 0$

- Q.4 Solve $x^2 + x - 4 + \frac{1}{x} + \frac{1}{x^2} = 0$
- Q.5 Solve $4 \cdot 2^{2x+1} - 9 \cdot 2^x + 1 = 0$
- Q.6 Solve $3^{2x-1} - 12 \cdot 3^x + 81 = 0$
- Q.7 Show that $(1 + \omega)(1 + \omega^2)(1 + \omega^4)(1 + \omega^8) \dots 2n \text{ factors} = 1$
- Q.8 Find the condition that one root of $ax^2 + bx + c = 0$, $a \neq 0$ is square of the other.
- Q.9 $x^3 + y^3 + z^3 - 3xyz = (x + y + z)(x + \omega y + \omega^2 z)(x + \omega^2 y + \omega z)$
- Q.10 If the roots of $px^2 + qx + r = 0$ are α and β , prove that $\sqrt{\frac{\alpha}{\beta}} + \sqrt{\frac{\beta}{\alpha}} + \sqrt{\frac{q}{p}} = 0$
- Q.11 If α, β are the roots of $5x^2 - x - 2 = 0$ form the equation whose roots are $\frac{3}{\alpha}$ and $\frac{3}{\beta}$.
- Q.12 Show that the roots of $x^2 + (mx + c)^2 = a^2$ will be equal if $c^2 = a^2(1 + m^2)$.
- Q.13 Show that the roots of $(mx + c)^2 = 4ax$ will be equal if $c = \frac{a}{m}$; $m \neq 0$
- Q.14 Prove that will have equal roots if $\frac{x^2}{a^2} + \frac{(mx+c)^2}{b^2} = 1$ will have equal roots if $c^2 = a^2m^2 + b^2$; $a \neq 0, b \neq 0$
- Q.15 Solve $3x + 4y = 25$; $\frac{x}{2} + \frac{y}{3} = 2$
- Q.16 Solve the system of equation : $x + y = a + b$ and $\frac{a}{x} + \frac{b}{y} = 2$
- Q.17 Prove that sum of three cube roots of unity is zero.
- Q.18 Prove that $(-1 + \sqrt{-3})^4 + (-1 - \sqrt{-3})^4 = -16$
- Q.19 If α, β are the roots of $5x^2 - x - 2 = 0$, form the equation whose roots are $\frac{3}{\alpha}$ and $\frac{3}{\beta}$
- Q.20 Solve $x^2 + (y + 1)^2 = 18$; $(x + 2)^2 + y^2 = 21$

Chapter 6:

- Q.1 Find n so that $\frac{a^n + b^n}{a^{n+1} + b^{n+1}}$ may be the A.M. between a and b.
- Q.2 The sum of 9 terms of an A.P. is 171 and its eight term is 31. Find the series.
- Q.3 The sum of three numbers in an A.P. is 24 and their product is 440. Find the numbers.
- Q.4 Find the four numbers in A.P. whose sum is 32 and the sum of whose squares is 276.
- Q.5 Find three consecutive numbers in G.P. whose sum is 26 and their product is 216.
- Q.6 Show that the reciprocals of the terms of the terms of the geometric sequence $a_1, a_1 r^2, a_1 r^4, \dots$ from another geometric sequence.
- Q.7 If the sum of the four consecutive terms in G.P. is 80 and A.M. of the second and the fourth of them is 30. Find the terms.
- Q.8 If a, b, c, d are in G.P. prove that $a^2 - b^2, b^2 - c^2, c^2 - a^2$ are in G.P. Q.9 For what value of n, is $\frac{a^n + b^n}{a^{n-1} + b^{n-1}}$ the positive geometric mean between two distinct numbers a and b ?
- Q.10 If $y = \frac{x}{2} + \frac{1}{4}x^2 + \frac{1}{8}x^3 + \dots$ and if $0 < x < 2$, then prove that $x = \frac{2y}{1+y}$
- Q.11 If $y = \frac{2}{3}x + \frac{4}{9}x^2 + \frac{8}{27}x^3 + \dots$ and if $0 < x < \frac{3}{2}$, then prove that $x = \frac{3y}{2(1+y)}$
- Q.12 Find the five numbers in A.P. whose sum is 25 and sum of whose Squares is 135.
- Q.13 If S_2, S_3, S_5 are the sums of $2n, 3n, 5n$ terms of an A.P., show that $S_5 = 5(S_3 - S_2)$
- Q.14 Show that the sum of n A.Ms. between a and b is equal to n times their A.M.
- Q.15 If $y = 1 + \frac{x}{2} + \frac{x^2}{4} + \dots$ then show that $x = 2\left(\frac{y-1}{y}\right)$
- Q.16 The sum of an infinite geometric series is 9 and the sum of the squares of its terms is $\frac{81}{5}$. Find the series.

Chapter 7:

- Q.1 Find the numbers greater than 23000 that can be formed from the digits 1, 2, 3, 5, 6 without repeating any digits.
- Q.2 How many 6-digit numbers can be formed without repeating any digit from the digits 0, 1, 2, 3, 4, 5 ? In how many of them will 0 be at the tens place?
- Q.3 Prove that ${}^n C_r + {}^n C_{r-1} = {}^{n+1} C_r$
- Q.4 How many 5-digit numbers can be formed from the digits 2, 2, 3, 3, 4, 4? How many of them will lie between 400,000 and 430,000 ?
- Q.5 In how many ways can the letters of the word MISSISSIPPI be arranged when all the letters are to be used?
- Q.6 Prove from the first principle that
- ii) ${}^n P_r = {}^{n-1} P_r + r \cdot {}^{n-1} P_{r-1}$

i) ${}^n P_r = n \cdot {}^{n-1} P_{r-1}$ Q.7 Find the value of n when

ii) ${}^{11} P_n = 11 \cdot 10 \cdot 9$

i) ${}^n P_2 = 30$

Q.8 How many numbers greater than 1000,000 can be formed from the digits 0,2,2,2,3,4,4?

Q.9 Find the value of n and r , when ${}^n C_r = 35$ and ${}^n P_r = 210$

Chapter 8:

Q.1 Use mathematical induction to prove that

i) $1 + 3 + 5 + \dots + (2n - 1) = n^2$

ii) $1 + 4 + 7 + \dots + (3n - 2) = \frac{n(3n-1)}{2}$

iii) $1 + 5 + 9 + \dots + (4n - 3) = n(2n - 1)$

Q.2 Find the term independent of x in the expansion

ii) $\left(x - \frac{2}{x}\right)^{10}$

i) $\left(\sqrt{x} + \frac{1}{2x}\right)^{10}$

Q.3 Find the term involving x^4 in the expansion of $(3 - 2x)^7$

Q.4 Use binomial theorem to show that $1 + \frac{1}{4} + \frac{1.3}{4.8} + \frac{1.3.5}{2.4.6} + \dots = \sqrt{2}$

Q.5 If x is so small that its square and higher powers can be neglected, then show that

$$\frac{1-x}{\sqrt{1+x}} = 1 - \frac{3}{2}x$$

Q.6 If $y = \frac{1}{3} + \frac{1.3}{2!} \left(\frac{1}{3}\right)^2 + \dots$, then prove that $y^2 + 2y - 2 = 0$

Q.7 Find the coefficient of x^5 in the expansion of $\left(x^2 - \frac{3}{2x}\right)^{10}$

Q.8 If x is very nearly equal to 1, then prove that $px^p - qx^q = (p - q)x^{p+q}$

Q.9 Find the term involving x^{-2} in the expression of $\left(x - \frac{2}{x^2}\right)^{13}$

Q.10 Determine the middle term or terms in the following expansions $\left(\frac{3}{2}x - \frac{1}{3x}\right)^{11}$ Q.11 If x is so small that its square and higher powers can be neglected, then show that

$$\frac{1+x}{\sqrt{1-x}} = 1 + \frac{3}{2}x$$

Q.12 If $2y = \frac{1}{2^2} + \frac{1.3}{2!} \frac{1}{2^4} + \frac{1.3.5}{3!} \frac{1}{2^6} + \dots$, then prove that $4y^2 + 4y - 1 = 0$

Chapter 9

Q.1 If $\cot \theta = \frac{15}{8}$ and the terminal arm of the angle is not in first quadrant, find the value $\cos \theta$ and $\operatorname{cosec} \theta$.

Q.2 If $\operatorname{cosec} \theta = \frac{m^2+1}{2m}$ and $0 < \theta < \frac{\pi}{2}$ find the value of the remaining trigonometric ratio.

Q.3 Prove the identity $\frac{1}{\operatorname{cosec} \theta - \cot \theta} - \frac{1}{\sin \theta} = \frac{1}{\sin \theta} - \frac{1}{\operatorname{cosec} \theta + \cot \theta}$

Q.4 Prove that $\frac{\tan \theta + \sec \theta - 1}{\tan \theta + \sec \theta + 1} = \tan \theta + \sec \theta$

Q.5 Prove that $\frac{1 - \sin \theta}{\cos \theta} = \frac{\cos \theta}{1 + \sin \theta}$

Q.6 $\sin^6 \theta - \cos^6 \theta = (\sin^2 \theta - \cos^2 \theta)(1 - \sin^2 \theta \cos^2 \theta)$

Q.7 $\sin^6 \theta + \cos^6 \theta = 1 - 3\sin^2 \theta \cos^2 \theta$

Q.8 If $\tan \theta = \frac{1}{\sqrt{7}}$ and the terminal arm of the angle is not in the I quadrant, find the value of $\frac{\sec^2 \theta - \sec^2 \theta}{\csc^2 \theta + \sec^2 \theta} = \frac{3}{4}$.

Q.9 Find the value of the other five trigonometric functions of θ , if $\cos \theta = \frac{12}{13}$ and the terminal side of the angle is not in the I quadrant.

Q.10 Prove that $(\tan \theta + \cot \theta)^2 = \sec^2 \theta \operatorname{csc}^2 \theta$

Q.11 If $\cot \theta = \frac{3}{2}$ and terminal arm of the angle is in the first quadrant, find the value of $\frac{3\sin \theta + 4\cos \theta}{\cos \theta - \sin \theta}$

Chapter 10

Q.1 Prove the identity $\frac{\sin 3\theta}{\sin \theta} - \frac{\cos 3\theta}{\cos \theta} = 2$

Q.2 If $\sin \alpha = \frac{4}{5}$ and $\sin \beta = \frac{40}{41}$, where $0 < \alpha < \frac{\pi}{2}$ and $0 < \beta < \frac{\pi}{2}$ Show that $\sin(\alpha - \beta) = \frac{113}{205}$

Q.3 Reduce $\cos^4 \theta$ to an expression involving only function of multiple of θ , raised to the first power.

$$Q.4 \sqrt{\frac{1+\sin \alpha}{1-\sin \alpha}} = \frac{\sin \frac{\alpha}{2} + \cos \frac{\alpha}{2}}{\sin \frac{\alpha}{2} - \cos \frac{\alpha}{2}}$$

$$Q.5 \text{ Show that } \cot(\alpha + \beta) = \frac{\cot \alpha \cot \beta - 1}{\cot \alpha + \cot \beta}$$

Q.6 Reduce $\sin^4 \theta$ to an expression involving only function of multiple of θ , raised to the first power.

$$Q.7 \text{ Prove that } \frac{\sin \theta + \sin 3\theta + \sin 5\theta + \sin 7\theta}{\cos \theta + \cos 3\theta + \cos 5\theta + \cos 7\theta} = \tan 4\theta$$

$$Q.8 \text{ Prove that } \cos 20^\circ \cos 40^\circ \cos 60^\circ \cos 80^\circ = \frac{1}{16}$$

$$Q.9 \text{ Prove that } \sin \frac{\pi}{9} \sin \frac{2\pi}{9} \sin \frac{\pi}{3} \sin \frac{4\pi}{9} = \frac{3}{16}$$

$$Q.10 \text{ Prove that } \sin 10^\circ \sin 30^\circ \sin 50^\circ \sin 70^\circ = \frac{1}{16}$$

$$Q.11 \text{ Prove that } \frac{\cos 8^\circ - \sin 8^\circ}{\cos 8^\circ + \sin 8^\circ} = \tan 37^\circ$$

$$Q.12 \text{ If } \alpha, \beta, \gamma \text{ are the angles of triangle ABC, show that } \cot \frac{\alpha}{2} + \cot \frac{\beta}{2} + \cot \frac{\gamma}{2} = \cot \frac{\alpha}{2} \cot \frac{\beta}{2} \cot \frac{\gamma}{2}$$

$$Q.13 \text{ Prove that } \frac{\sin A + \sin 2A}{1 + \cos A + \cos 2A} = \tan A$$

$$Q.14 \text{ Show that } \cos(\alpha + \beta) \cos(\alpha - \beta) = \cos^2 \alpha - \sin^2 \beta = \cos^2 \beta - \sin^2 \alpha$$

Chapter 12

Q.1 Solve the triangle ABC, in which $a = 3, c = 6, \beta = 36^\circ 20'$

Q.2 Solve the triangle ABC, in which $a = 7, b = 3, \gamma = 38^\circ 13'$

Q.3 Solve the triangle ABC, in which $a = 32, b = 40, c = 66$

Q.4 The sides of triangle are $x^2 + x + 1, 2x + 1$ and $x^2 - 1$. Prove that the greatest angle of the triangle is 120° .

$$Q.5 \text{ Show that } r = a \sin \frac{\beta}{2} \sin \frac{\gamma}{2} \sec \frac{\alpha}{2}$$

$$Q.6 \text{ Show that } r_1 = 4R \sin \frac{\alpha}{2} \cos \frac{\beta}{2} \cos \frac{\gamma}{2}$$

$$Q.7 \text{ Show that } r_1 = s \tan \frac{\alpha}{2}$$

Q.8 Prove that in equilateral triangle $r: R: r_1 = 1: 2: 3$

$$Q.9 \text{ Prove that } r = s \tan \frac{\alpha}{2} \tan \frac{\beta}{2} \tan \frac{\gamma}{2}$$

$$Q.10 \text{ Prove that } (r_1 + r_2) \tan \frac{\gamma}{2} = c$$

$$Q.11 \text{ With usual notations, prove that } R = \frac{abc}{4\Delta}$$

$$Q.12 \text{ With usual notations, prove that } r = \frac{\Delta}{s}$$

Q.13 Prove that Law of Cosine.

Q.14 Prove that Law of Sine.

$$Q.15 \text{ Show that } r = (s - a) \tan \frac{\alpha}{2} = (s - b) \tan \frac{\beta}{2} = (s - c) \tan \frac{\gamma}{2}$$

Q.16 Prove that $abc(\sin \alpha + \sin \beta + \sin \gamma) = 4\Delta s$.

Q.17 Prove that $r_1 r_2 + r_2 r_3 + r_3 r_1 = s^2$

Q.18 Prove that $r_1 + r_2 + r_3 - r = 4R$

Chapter 13

$$Q.1 \text{ Prove that } \sin^{-1} \frac{5}{13} + \sin^{-1} \frac{7}{25} = \cos^{-1} \frac{253}{325}$$

$$Q.2 \text{ prove that } \sin^{-1} \frac{3}{5} + \sin^{-1} \frac{8}{17} = \sin^{-1} \frac{77}{85}$$

$$Q.3 \text{ Prove that } \sin^{-1} \frac{1}{\sqrt{5}} + \cot^{-1} 5 = \frac{\pi}{4}$$

$$Q.4 \text{ Prove that } \tan^{-1} \frac{3}{4} + \tan^{-1} \frac{1}{5} - \tan^{-1} \frac{8}{17} = \frac{\pi}{4}$$

$$Q.5 \text{ Prove that } \sin^{-1} A + \sin^{-1} B = \sin^{-1} (A\sqrt{1-B^2} + B\sqrt{1-A^2})$$

$$Q.6 \text{ Prove that } \sin^{-1} \frac{17}{85} - \sin^{-1} \frac{1}{5} = \cos^{-1} \frac{17}{17}$$

$$Q.7 \text{ Prove that } \tan^{-1} \frac{1}{11} + \tan^{-1} \frac{5}{6} = \tan^{-1} \frac{1}{3} + \tan^{-1} \frac{1}{2}$$

$$Q.8 \text{ Prove that } 2 \tan^{-1} \frac{1}{3} + \tan^{-1} \frac{1}{7} = \frac{\pi}{4}$$