

- (a)  $\underline{u} \times \underline{v}$  (b)  $|\underline{u} \times \underline{v}|$  (c)  $\frac{1}{2}(\underline{u} \times \underline{v})$  (d)  $\checkmark \frac{1}{2}|\underline{u} \times \underline{v}|$
216. The scalar triple product of  $\underline{a}$ ,  $\underline{b}$  and  $\underline{c}$  is denoted by  
 (a)  $\underline{a} \cdot \underline{b} \cdot \underline{c}$  (b)  $\checkmark \underline{a} \cdot \underline{b} \times \underline{c}$  (c)  $\underline{a} \times \underline{b} \times \underline{c}$  (d)  $(\underline{a} + \underline{b}) \times \underline{c}$
217. Cross product or vector product is defined  
 (b) In plane only (b)  $\checkmark$  in space only (c) everywhere (d) in vector field
218. If  $\underline{u}$  and  $\underline{v}$  are two vectors, then  $\underline{u} \times \underline{v}$  is a vector  
 (b) Parallel to  $\underline{u}$  and  $\underline{v}$  (b) parallel to  $\underline{u}$  (c)  $\checkmark$  perpendicular to  $\underline{u}$  and  $\underline{v}$  (d) orthogonal to  $\underline{u}$
219. If  $\underline{u}$  and  $\underline{v}$  be any two vectors, along the adjacent sides of ||gram then the area of ||gram is  
 (b)  $\underline{u} \times \underline{v}$  (b)  $\checkmark |\underline{u} \times \underline{v}|$  (c)  $\frac{1}{2}(\underline{u} \times \underline{v})$  (d)  $\frac{1}{2}|\underline{u} \times \underline{v}|$
220. If  $\underline{u}$  and  $\underline{v}$  be any two vectors, along the adjacent sides of triangle then the area of triangle is  
 (b)  $\underline{u} \times \underline{v}$  (b)  $|\underline{u} \times \underline{v}|$  (c)  $\frac{1}{2}(\underline{u} \times \underline{v})$  (d)  $\checkmark \frac{1}{2}|\underline{u} \times \underline{v}|$
221. Two non zero vectors are perpendicular iff  
 (a)  $\underline{u} \cdot \underline{v} = 1$  (b)  $\underline{u} \cdot \underline{v} \neq 1$  (c)  $\underline{u} \cdot \underline{v} \neq 0$  (d)  $\checkmark \underline{u} \cdot \underline{v} = 0$
222. The scalar triple product of  $\underline{a}$ ,  $\underline{b}$  and  $\underline{c}$  is denoted by  
 (b)  $\underline{a} \cdot \underline{b} \cdot \underline{c}$  (b)  $\checkmark \underline{a} \cdot \underline{b} \times \underline{c}$  (c)  $\underline{a} \times \underline{b} \times \underline{c}$  (d)  $(\underline{a} + \underline{b}) \times \underline{c}$
223. The vector triple product of  $\underline{a}$ ,  $\underline{b}$  and  $\underline{c}$  is denoted by  
 (a)  $\underline{a} \cdot \underline{b} \cdot \underline{c}$  (b)  $\underline{a} \cdot \underline{b} \times \underline{c}$  (c)  $\checkmark \underline{a} \times \underline{b} \times \underline{c}$  (d)  $(\underline{a} + \underline{b}) \times \underline{c}$
224. Notation for scalar triple product of  $\underline{a}$ ,  $\underline{b}$  and  $\underline{c}$  is  
 (a)  $\underline{a} \cdot \underline{b} \times \underline{c}$  (b)  $\underline{a} \times \underline{b} \cdot \underline{c}$  (c)  $[\underline{a} \cdot \underline{b} \cdot \underline{c}]$  (d)  $\checkmark$  all of these
225. If the scalar product of three vectors is zero, then vectors are  
 (a) Collinear (b)  $\checkmark$  coplanar (c) non coplanar (d) non-collinear
226. If any two vectors of scalar triple product are equal, then its value is equal to  
 (a) 1 (b)  $\checkmark$  0 (c) -1 (d) 2
227. Moment of a force  $\underline{F}$  about a point is given by:  
 (a) Dot product (b)  $\checkmark$  cross product (c) both (a) and (b) (d) None of these

## Q.NO.2

1.  $x = at^2, y = 2at$  represent the equation of parabola  $y^2 = 4ax$
2. Express the perimeter  $P$  of square as a function of its area  $A$ .
3. Show that  $x = a \cos \theta, y = b \sin \theta$  represent the equation of ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$
4. Show that:  $\sinh 2x = 2 \sinh x \cosh x$   
Express the volume  $V$  of a cube as a function of the area  $A$  of its base.
5. Find  $\frac{f(a+h)-f(a)}{h}$  and simplify  $f(x) = \cos x$
6.  $f(x) = \frac{1}{\sqrt{x-1}}, x \neq 1; g(x) = (x^2 + 1)^2$
7. (a)  $f^{-1}(x)$  (b)  $f^{-1}(-1)$  and verify  $f(f^{-1}(x)) = f^{-1}(f(x)) = xf(x) = \frac{2x+1}{x-1}, x > 1$
8. Show that  $\lim_{x \rightarrow 0} \frac{a^x - 1}{x} = \log_e a$
9. Evaluate  $\lim_{x \rightarrow 0} \frac{\sin 7x}{x}$
10. Evaluate  $\lim_{n \rightarrow +\infty} \left(1 + \frac{1}{n}\right)^n$
11.  $\lim_{h \rightarrow 0} \frac{\sqrt{x+h} - \sqrt{x}}{h}$
12.  $\lim_{x \rightarrow 0} (1 + 2x^2)^{\frac{1}{x^2}}$
13. Evaluate  $\lim_{\theta \rightarrow 0} \frac{1 - \cos \theta}{\theta}$
14. Evaluate  $\lim_{x \rightarrow 0} \frac{x^n - a^n}{x^m - a^m}$

15.  $\lim_{x \rightarrow 0} \frac{e^{1/x} - 1}{e^{1/x} + 1}, x > 0$
16. (i)  $\lim_{x \rightarrow 0} \frac{\sin x^0}{x}$  (ii)  $\lim_{\theta \rightarrow 0} \frac{1 - \cos \theta}{\sin \theta}$  (iii)  $\lim_{x \rightarrow 0} \frac{\sin ax}{\sin bx}$
17. Discuss the continuity of the function at  $x = 3$   $g(x) = \frac{x^2 - 9}{x - 3}$  if  $x \neq 3$
18. Discuss the continuity of  $f(x)$  at  $x = c$ .  $f(x) = \begin{cases} 2x + 5 & \text{if } x \leq 2 \\ 4x + 1 & \text{if } x > 2 \end{cases}$   $c = 2$
19. Discuss the continuity of  $f(x)$  at 3, when  $f(x) = \begin{cases} x - 1 & \text{if } x \leq 3 \\ 2x + 1 & \text{if } 3 < x \end{cases}$
20. Find the derivative of the given function by definition  $f(x) = x^2$
21. Find the derivative of the given function by definition  $f(x) = \frac{1}{\sqrt{x}}$
22. Find the derivative of  $y = (2\sqrt{x} + 2)(x - \sqrt{x})$  w.r.t 'x'
23. Differentiate  $\frac{2x^3 - 3x^2 + 5}{x^2 + 1}$  w.r.t 'x'
24. If  $x^4 + 2x^2 + 2$ , Prove that  $\frac{dy}{dx} = 4x\sqrt{y - 1}$
25. Differentiate  $(\sqrt{x} - \frac{1}{\sqrt{x}})^2$  w.r.t 'x'.
26. Differentiate  $(x - 5)(3 - x)$
27. Find  $\frac{dy}{dx}$  if  $x = \theta + \frac{1}{\theta}, y = \theta + 1$
28. Find  $\frac{dy}{dx}$  by making some suitable substitution if  $y = \sqrt{x + \sqrt{x}}$
29. Differentiate  $x^2 + \frac{1}{x^2}$  w.r.t  $x - \frac{1}{x}$
30. Find  $\frac{dy}{dx}$  if  $y^2 - xy - x^2 + 4 = 0$
31. Find  $\frac{dy}{dx}$  if  $x^2 + y^2 = 4$
32. Find  $\frac{dy}{dx}$  if  $y = x^n$  where  $n = \frac{p}{q}, q \neq 0$
33. If  $y = (ax + b)^n$  where  $n$  is negative integer, find  $\frac{dy}{dx}$  using quotient theorem.
34. Find  $\frac{dy}{dx}$  if  $xy + y^2 = 2$
35. Differentiate  $(1 + x^2)$  w.r.t  $x^2$
36. Find  $\frac{dy}{dx}$  if  $3x + 4y + 7 = 0$
37. Find  $\frac{dy}{dx}$  if  $y = x \cos y$
38. Differentiate  $\sin^2 x$  w.r.t  $\cos^2 x$
39. Find  $f'(x)$  if  $f(x) = \ln(e^x + e^{-x})$
40. Find  $f'(x)$  if  $f(x) = e^x (1 + \ln x)$
41. Differentiate  $(\ln x)^x$  w.r.t 'x'
42. Find  $\frac{dy}{dx}$  if  $y = a^{\sqrt{x}}$
43. Find  $\frac{dy}{dx}$  if  $y = 5e^{3x-4}$
44. Find  $\frac{dy}{dx}$  if  $y = (x + 1)^x$
45. Find  $\frac{dy}{dx}$  if  $y = xe^{x \ln x}$
46. Find  $\frac{dy}{dx}$  if  $y = (\ln \tan x)$
47. Find  $\frac{dy}{dx}$  if  $y = \sinh^{-1}(\frac{x}{2})$
48. Find  $\frac{dy}{dx}$  if  $y = \tanh^{-1}(\sin x)$  ,  $-\frac{\pi}{2} < x < \frac{\pi}{2}$
49. If  $y = \sin^{-1} \frac{x}{a}$ , then show that  $y_2 = x(a^2 - x^2)^{-\frac{3}{2}}$
50. Find  $y_2$  if  $y = x^2 \cdot e^{-x}$
51. Find  $y_2$  if  $x = a \cos \theta, y = \sin \theta$
52. Find  $y_2$  if  $x^3 - y^3 = a^3$
53. Find the first four derivatives of  $\cos(ax + b)$

54. Apply Maclaurin's Series expansion to prove that  $e^{2x} = 1 + 2x + \frac{4x^2}{2!} + \frac{8x^3}{3!} + \dots$
55. Apply Maclaurin's Series expansion to prove that  $e^x = 1 + x + \frac{x^2}{2!} + \dots$
56. State Taylor's series expansion.
57. Expand  $\cos x$  by Maclaurin's series expansion.
58. Define Increasing and decreasing functions.
59. Determine the interval in which  $f(x) = x^2 + 3x + 2; x \in [-4, 1]$
60. Determine the interval in which  $f(x) = \cos x; x \in \left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$
61. Find the extreme values of the function  $f(x) = 3x^2 - 4x + 5$
62. Find the extreme values of the function  $f(x) = 1 + x^3$
63. Find  $\delta y$  and  $\Delta y$  if  $y = x^2 + 2x$  when  $x$  changes from 2 to 1.8
64. Use differentials find  $\frac{dy}{dx}$  and  $\frac{dx}{dy}$  in the following equations.
65.  $xy + x = 4$  (b)  $xy - \ln x = c$
66. Find the approximate increase in the volume of a cube if the length of its each edge changes from 5 to 5.02
67. Find the approximate increase in the area of a circular disc if its diameter is increased from 44cm to 44.4cm.

## Q.NO.3

1. Find  $dy$  in  $y = x^2 + 2x$  when  $x$  changes from 2 to 1.8 .
2. If  $xy + x = 4$ , find  $\frac{dx}{dy}$  by using differentials.
3. Using differentials find  $\frac{dx}{dy}$   $xy - \ln x = c$ .
4. Use differential to approximate the value of  $\cos 29^\circ$
5. Evaluate  $\tan^2 \int x dx$ .
6. Find  $\int a^{x^2} x dx$
7. Evaluate  $\int \cos 3x \sin 2x dx$ .
8. Evaluate  $\int \frac{ax+b}{ax^2+2bx+c} dx$
9. Evaluate  $\int \sqrt{1 - \cos 2x} dx, (1 - \cos 2x) > 0$ .
10. Evaluate  $\int \frac{\sec^2 x}{\sqrt{\tan x}} dx$
11. Evaluate  $\int \frac{e^{2x} + e^x}{e^x} dx$
12. Integrate by substitution  $\int \frac{-2x}{\sqrt{4-x^2}} dx$ .
13. Find the integral  $\int \frac{\cos x}{\sin x \ln(\sin x)} dx$
14. Evaluate  $\int \frac{1}{x \ln x} dx$ .
15. Evaluate  $\int \frac{2x}{1 - \sin x} dx$
16. Evaluate  $\int \frac{e^x(1+x)}{(2+x)^2} dx$
17. Evaluate  $\int x \ln x dx$
18. Evaluate  $\int \frac{3-x}{1-x+6x^2} dx$
19. Evaluate  $\int_{-1}^3 (x^3 + 3x^2) dx$ .
20.  $\int_0^{\frac{\pi}{6}} x \cos x dx$
21. Solve the differential equations  $\frac{dy}{dx} = \frac{y^2+1}{e^{-x}}$ .
22. Write two properties of definite integral.
23. Find the area between the  $x$ -axis and curve  $y = 4x - x^2$

24. Solve the differential equation  $\frac{x^2+1}{y+1} = \frac{x}{y} \frac{dy}{dx}$
25. Evaluate  $\int \frac{1}{\sqrt{x+1}-\sqrt{x}} dx$
26. Evaluate  $\int \frac{dx}{x(\ln 2x)^3} x > 0$
27. Evaluate  $\int x^5 \ln x dx$
28. Evaluate  $\int \frac{2a}{a^2-x^2} dx, x < a$
29. Evaluate  $\int_{-1}^2 (x + |x|) dx$
30. Evaluate  $\int_0^3 \frac{dx}{x^2+9}$
31. Evaluate  $\int \tan^{-1} x dx$
32. Evaluate  $\int_2^{\sqrt{5}} x \sqrt{x^2-1} dx$
33. Evaluate  $\int \frac{e^{\tan^{-1} x}}{1+x^2} dx$
34. Evaluate  $\int x^2 \ln x dx$
35. Evaluate integral  $\int x \cdot \sin x dx$
36. Find indefinite integral  $\int e^{ax} \left[ a \sec^{-1} x + \frac{1}{x\sqrt{x^2-1}} \right] dx$
37. Evaluate  $\int \frac{5x+8}{(x+3)(2x-1)} dx$  by using partial fraction
38. Solve  $x^2(2y+1) \frac{dy}{dx} - 1 = 0$ .
39. Show that  $y = \tan(e^x + c)$  is solution of  $\frac{dy}{dx} = \frac{y^2+1}{e^{-x}}$
40. Evaluate  $\int_{\frac{\pi}{6}}^{\frac{\pi}{3}} \cos t dt$ .
41. What is differential coefficient?
42. Define Definite integral.
43. Define integral
44. Calculate the integral  $\int_0^{\frac{\pi}{4}} \sec x (\sec x + \tan x) dx$ .
45. If  $\int_{-2}^1 f(x) dx = 5$ ,  $\int_{-2}^1 g(x) dx = 4$  then Evaluate  $\int_{-2}^1 [3f(x) - 2g(x)] dx$
46. Show that the points  $A(3, 1)$ ,  $B(-2, -3)$  and  $C(2, 2)$  are vertices of an isosceles triangle.
47. Find the mid-point of the line segment joining the vertices  $A(-8, 3)$ ,  $B(2, -1)$ .
48. Show that the vertices  $(-1, 2)$ ,  $B(7, 5)$ ,  $C(2, -6)$  are vertices of a right triangle.
49. Find the points trisecting the join of  $A(-1, -4)$  and  $B(6, 2)$ .
50. Find  $h$  such that  $(-1, h)$ ,  $B(3, 2)$ , and  $C(7, 3)$  are collinear.
51. Describe the location in the plane of point  $P(x, y)$  for which  $x = y$ .
52. The point  $C(-5, 3)$  is the centre of a circle and  $P(7, -2)$  lies on the circle. What is the radius of the circle?
53. Find the point three-fifth of the way along the line segment from  $A(-5, 8)$  to  $B(5, 3)$ .
54. The two points  $P$  and  $O'$  are given in  $xy$ -coordinate system. Find the  $X'Y'$ -coordinates of  $P$  referred to the translated axes  $O'X'$  and  $O'Y'$  if  $P(-2, 6)$  and  $O'(-3, 2)$ .
55. The  $xy$ -coordinate axes are translated through point  $O'$  whose coordinates are given in  $xy$ -coordinate system. The coordinates of  $P$  are given in the  $XY$ -coordinate system. Find the coordinates of  $P$  in  $xy$ -coordinate system if  $(-5, -3)$ ,  $O'(-2, 3)$ .
56. What are translated axes.
57. Show that the points  $A(-3, 6)$ ,  $B(3, 2)$  and  $C(6, 0)$  are collinear.
58. Find an equation of the straight line if its slope is 2 and  $y$ -axis is 5.
59. Find the slope and inclination of the line joining the points  $(-2, 4)$ ;  $(5, 11)$
60. Find  $k$  so that the line joining  $A(7, 3)$ ;  $B(k, -6)$  and the line joining  $C(-4, 5)$ ;  $D(-6, 4)$  are perpendicular.
61. Find an equation of the line bisecting the I and III quadrants.
62. Find an equation of the line for  $x$ -intercept:  $-3$  and  $y$ -intercept:  $4$
63. Find the distance from the point  $P(6, -1)$  to the line  $6x - 4y + 9 = 0$
64. Find whether the given point  $(5, 8)$  lies above or below the line  $2x - 3y + 6 = 0$

65. Check whether the lines are concurrent or not.  
 $3x - 4y - 3 = 0$ ;  $5x + 12y + 1 = 0$ ;  $32x + 4y - 17 = 0$
66. Transform the equation  $5x - 12y + 39 = 0$  to "Two-intercept form".
67. Find the point of intersection of the lines  $x - 2y + 1 = 0$  and  $2x - y + 2 = 0$ .
68. Find an equation of the line through the point  $(2, -9)$  and the intersection of the lines  $2x + 5y - 8 = 0$  and  $3x - 4y - 6 = 0$ .
69. Determine the value of  $p$  such that the lines  $2x - 3y - 1 = 0$ ,  $3x - y - 5 = 0$  and  $3x + py + 8 = 0$  meet at a point.
70. Find the angle measured from the line  $l_1$  to the line  $l_2$  where  $l_1$ : Joining  $(2, 7)$  and  $(7, 10)$   
 $l_2$ : Joining  $(1, 1)$  and  $(-5, 5)$
71. Express the given system of equations in matrix form  $2x + 3y + 4 = 0$ ;  $x - 2y - 3 = 0$ ;  $3x + y - 8 = 0$
72. Find the angle from the line with slope  $-\frac{7}{3}$  to the line with slope  $\frac{5}{2}$ .
73. Find an equation of each of the lines represented by  $20x^2 + 17xy - 24y^2 = 0$
74. Define Homogenous equation.
75. Write down the joint equation.

## Q.NO.4

1. Find a joint equation of the straight lines through the origin perpendicular to the lines represented by  $x^2 + xy - 6y^2 = 0$ .
2. Find measure of angle between the lines represented by  $x^2 - xy - 6y^2 = 0$ .
3. Define "Corner Point" or "Vertex".
4. Graph the solution set of linear inequality  $3x + 7y \geq 21$ .
5. Indicate the solution set of  $3x + 7y \geq 21$ ;  $x - y \leq 2$
6. What is "Corresponding equation".
7. Graph the inequality  $x + 2y < 6$ .
8. Graph the feasible region of  $x + y \leq 5$ ;  $-2x + y \leq 0$   $x \geq 0$ ;  $y \geq 0$
9. Graph the feasible region of  $5x + 7y \leq 35$ ;  $x - 2y \leq 4$   $x \geq 0$ ;  $y \geq 0$
10. Define "Feasible region".
11. Graph the feasible region of  $2x - 3y \leq 6$ ;  $2x + y \geq 2$   $x \geq 0$ ;  $y \geq 0$
12.  $\underline{a} = 3\underline{i} - 2\underline{j} + \underline{k}$ ,  $\underline{b} = \underline{i} + \underline{j}$ , find  $\underline{b} \times \underline{a}$
13. A force  $\underline{F} = 7\underline{i} + 4\underline{j} - 3\underline{k}$  is applied at  $P(1, -2, 3)$ . Find its moment about the point  $Q(2, 1, 1)$ .
14. By means of slope, show the points lie on the same line  $A(-1, -3)$ ,  $B(1, 5)$ ,  $C(2, 9)$
15. Calculate the projection of  $\underline{a}$  along  $\underline{b}$  when  $\underline{a} = \underline{i} + \underline{k}$ ,  $\underline{b} = \underline{j} + \underline{k}$
16. Check the position of the point  $(5, 6)$  with respect to the circle  $2x^2 + 2y^2 + 12x - 8y + 1 = 0$ .
17. Check whether  $(-2, 4)$  lies above or below  $4x + 5y - 3 = 0$
18. Check whether the point  $(-2, 4)$  lies above or below the line  $4x + 5y - 3 = 0$ .
19. Check whether the point  $(-4, 7)$  is above or below of the line  $6x - 7y + 70 = 0$ .
20. Convert  $2x - 4y + 11 = 0$  into slope intercept form.
21. Convert the equation  $4x + 7y - 2 = 0$  into two intercept form.
22. Convert the equation into two intercept form  $4x + 7y - 2 = 0$ .
23. Define direction angles and direction cosines of a vector
24. Define focal chord of parabola.
25. Define parabola.
26. Define trapezium.
27. Define unit vector.
28. Find a scalar "  $\alpha$  " so that the vectors  $2\underline{i} + \underline{a}\underline{j} + 5\underline{k}$  and  $3\underline{i} + \underline{j} + \alpha\underline{k}$  are perpendicular.
29. Find a vector of length 5, in the direction of opposite that of  $\underline{v} = \underline{i} - 2\underline{j} + 3\underline{k}$ .
30. Find a vector perpendicular to each of the vector  $\underline{a} = 2\underline{i} - \underline{j} - \underline{k}$  and  $\underline{b} = 4\underline{i} + 2\underline{j} - \underline{k}$ .

31. Find a vector perpendicular to each of the vectors  $= 2\hat{i} + \hat{j} + \hat{k}$  and  $= 4\hat{i} + 2\hat{j} - \hat{k}$ .
32. Find a vector whose magnitude is '4' and is parallel to  $2\hat{i} - 3\hat{j} + 6\hat{k}$ .
33. Find an equation of a line bisecting 2<sup>nd</sup> and 4<sup>th</sup> quadrants.
34. Find an equation of a line through the points  $(-2, 1)$  and  $(6, -4)$ .
35. Find an equation of a line with  $x$ -intercept: -9 and slope: -4.
36. Find an equation of hyperbola if its foci  $(0, \pm 9)$  and directrices  $y = \pm 4$ .
37. Find an equation of the line through  $(-4, -5)$  and perpendicular to the line having slope  $\frac{-3}{2}$ .
38. Find the angle from the line with slope  $\frac{-7}{3}$  to the line with slope  $\frac{5}{2}$ .
39. Find an equation of the line through  $(5, -8)$  and perpendicular to the join of  $A(-15, -8)$ ,  $B(10, -7)$ .
40. Find an equation of the line with  $x$ -intercept: -3 and  $y$ -intercept: 4.
41. Find an equation of the perpendicular bisector of the segment joining the points  $A(3, 5)$  and  $B(9, 8)$ .
42. Find an equation of the vertical line through  $(-5, 3)$ .
43. Find an unit vector in the direction of the vector  $v = \frac{1}{2}\hat{i} + \frac{\sqrt{3}}{2}\hat{j}$ .
44. Find centre and radius of circle  $5x^2 + 5y^2 + 14x + 12y - 10 = 0$ .
45. Find centre and vertices of ellipse  $\frac{(x-1)^2}{4} + \frac{(y-1)^2}{9} = 1$ .
46. Find condition that the lines  $y = m_1x + c_1$ ,  $y = m_2x + c_2$ ,  $y = m_3x + c_3$  are concurrent.
47. Find direction cosine of  $\underline{v} = 3\hat{i} - \hat{j} + 2\hat{k}$ .
48. Find eccentricity of the ellipse  $x^2 + 4y^2 = 16$ .
49. Find equation of hyperbola with foci  $(\pm 5, 0)$  and vertex of  $(3, 0)$ .
50. Find equation of latus rectum of parabola  $y^2 = -8(x - 3)$ .
51. Find focus and vertex of the parabola  $y = 6x^2 - 1$ .
52. Find  $h$  such that  $A(-1, h)$ ,  $B(3, 2)$  and  $C(7, 3)$  are collinear.
53. Find length of tangent segment from  $(-5, 4)$  to  $5x^2 + 5y^2 - 10x + 15y - 131 = 0$ .
54. Find measure of the angle between the lines represented by  $x^2 - xy - 6y^2 = 0$ .
55. Find point which divide  $A(-6, 3)$  and  $B(5, -2)$  internally in 2:3.
56. Find position vector of a point which divide the join of  $E$  with position vector  $5\hat{i}$  and  $F$  with position vector  $4\hat{i} + \hat{j}$  in ratio 2:5.
57. Find slope and inclination of the line joining points  $(4, 6)$ ,  $(4, 8)$ .
58. Find the angle between the vectors  $\underline{u} = 2\hat{i} - \hat{j} + \hat{k}$  and  $\underline{v} = -\hat{i} + \hat{j}$ .
59. Find the area of the triangle with vertices  $A(1, -1, 1)$ ,  $B(2, 1, -1)$  and  $C(-1, 1, 2)$ .
60. Find the centre and radius of the circle  $x^2 + y^2 + 12x - 10y = 0$ .
61. Find the coordinate of the points of the points of intersection of the line  $x + 2y = 6$  with the circle  $x^2 + y^2 - 2x - 2y - 39 = 0$ .
62. Find the coordinates of the points of intersection of the line  $2x + y = 5$  and  $x^2 + y^2 + 2x - 9 = 0$ .
63. Find the direction cosines for  $\overrightarrow{PQ}$ , where  $P(2, 1, 5)$ ,  $Q(1, 3, 4)$ .
64. Find the direction cosines of the vector  $6\hat{i} - 2\hat{j} + \hat{k}$ .
65. Find the distance from the point  $P(6, -1)$  to the line  $6x - 4y + 9 = 0$ .
66. Find the equation of ellipse when foci  $(\pm 3, 0)$  and minor axis of length 10.
67. Find the equation of the line through  $A(-6, 5)$  having slope 7.
68. Find the focus and directrix of the parabola  $y = 6x^2 - 1$ .
69. Find the focus and vertex of parabola  $(x - 1)^2 = 8(y + 2)$ .
70. Find the lines represented by  $20x^2 + 17xy - 24y^2 = 0$ .
71. Find the lines represented by  $x^2 - xy - 6y^2 = 0$ , also find the angle between them.
72. Find the measure of angle between the lines represented by  $x^2 - xy - 6y^2 = 0$ .
73. Find the mid-point of the line joining the two points  $A(-8, 3)$ ,  $B(2, 1)$ .
74. Find the point three-fifth of the way along line segment from  $A(-5, 8)$  to  $B(5, 3)$ .
75. Find the projection of vector  $\underline{a}$  along vector  $\underline{b}$  and projection of vector  $\underline{b}$  along when  $\underline{a} = \hat{i} - \hat{k}$ ,  $\underline{b} = \hat{j} + \hat{k}$ .
76. Find the value of  $3\hat{j} \cdot \hat{k} \times \underline{a}$ .
77. Find the value of  $2\hat{i} \times 2\hat{j} - \hat{k}$ .

78. Find unit vector perpendicular to the plane of  $\underline{a}$  and  $\underline{b}$  if  $\underline{a} = -\underline{i} - \underline{j} - \underline{k}$ ,  $\underline{b} = 2\underline{i} - 3\underline{j} + 4\underline{k}$ .
79. Find vertices and equation of directrices of hyperbola  $x^2 - y^2 = 9$ . 17Grp11,
80. Find  $\alpha$  so that  $\underline{u} = \alpha\underline{i} + 2\underline{a}\underline{j} - \underline{k}$  and  $\underline{v} = \underline{i} + \alpha\underline{j} + 3\underline{k}$  are perpendicular.
81. Find  $a$ , so that  $|\alpha\underline{i} + (a+1)\underline{j} + 2\underline{k}| = 3$ .
82. Find the value  $3\underline{j} \cdot \underline{k} \times \underline{i}$ .
83. If  $\overline{AB} = \overline{CD}$ , find coordinates of points A. If B, C, D are (1, 2), (-2, 5), (4, 1)
84. If  $\underline{a} = 2\underline{i} + \underline{j} - \underline{k}$  and  $\underline{b} = \underline{i} - \underline{j} + \underline{k}$  find the cross product  $\underline{a} \times \underline{b}$
85. If  $\underline{u} = 3\underline{i} + \underline{j} - \underline{k}$  and  $\underline{v} = 2\underline{i} - \underline{j} + \underline{k}$ , find the cosines of the angle  $\theta$  between  $\underline{u}$  and  $\underline{v}$
86. If O is the origin and  $\overrightarrow{OP} = \overline{AB}$ , find the point P when A and B are (-3, 7) and (1, 0) respectively
87. Prove that if  $\underline{a} + \underline{b} + \underline{c} = \underline{0}$  then  $\underline{a} \times \underline{b} = \underline{b} \times \underline{c} = \underline{c} \times \underline{a}$
88. Prove that  $\underline{a} \times (\underline{b} + \underline{c}) + \underline{b} \times (\underline{c} + \underline{a}) + \underline{c} \times (\underline{a} + \underline{b}) = \underline{0}$ .
89. Prove that if the lines are perpendicular, then product of their slopes = -1
90. Show that the points A(3, 1), B(-2, -3) and C(2, 2) are vertices of an isosceles triangle.
91. Show that the points A(-1, 2), B(7, 5) and C(2, -6) are vertices of a right triangle.
92. Show that the triangle with vertices A(1, 1), B(4, 5) and C(12, -5) is right triangle.
93. Show that vectors  $3\underline{i} - 2\underline{j} + \underline{k}$ ,  $\underline{i} - 3\underline{j} + 5\underline{k}$  and  $2\underline{i} + \underline{j} - 4\underline{k}$  form a right triangle.
94. Transform  $5x - 12y + 39 = 0$  into two intercept form. 15 Grp II,
95. Two lines  $l_1$  and  $l_2$  with respective slopes  $m_1$  and  $m_2$  are parallel if  $m_1 = m_2$ .
96. Write an equation of parabola with focus (-1, 0), vertex (-1, 2).
97. Write direction cosine of  $\overline{PQ}$ , if P(2, 1, 5), Q(1, 3, 1).
98. Write down the equation of straight line with x-intercept (2, 0) and y-intercept (0, -4)
99. Find the mid-point of line segment joining the points A  $(-\sqrt{5}, -\frac{1}{3})$  and  $(-3\sqrt{5}, 5)$ .
100. Find the slope and inclination of the line joining the points (-2, 4) and (5, 11).
101. Find equation of tangent to the circle  $x^2 + y^2 = 25$  at (4, 3).
102. Find the vertex and directrix of parabola  $x^2 = 4(y - 1)$ .
103. Find the centre and vertices of the ellipse  $9x^2 + y^3 = 18$ .
104. Find the sum of vectors  $\overline{AB}$  and  $\overline{CD}$ , given the four points A(1, -1), B(2, 0), C(-1, 3) and D(-2, 2).
105. Find a vector perpendicular to each of the vectors  $\underline{a} = 2\underline{i} + \underline{j} + \underline{k}$  and  $\underline{b} = 4\underline{i} + 2\underline{j} - \underline{k}$ .
106. Prove that the vectors  $\underline{i} - 2\underline{j} + 3\underline{k}$ ,  $2\underline{i} + 3\underline{j} - 4\underline{k}$  and  $\underline{i} - 3\underline{j} + 5\underline{k}$  are co-planar.
107. Find equation of a line through (-4, 7) and parallel to the line  $2x - 7y + 4 = 0$ .
108. Find equation of a line through (-6, 5) having slope = 7
109. Find distance from the point P (6, -1) to the line  $6x - 14y + 9 = 0$
110. Find area of triangular region whose vertices are A (5, 3), B (-2, 2), C (4, 2).
111. Find the equation of tangent to the circle  $x^2 + y^2 = 25$  at (4, 3). 14 Grp I,
112. Find the equation of parabola whose focus is (2, 5) and directrix is  $y = 1$
113. Find foci and eccentricity of ellipse
114. Find vector from A to origin whose  $\overline{AB} = 4\underline{i} - 2\underline{j}$  and B (-2, 5).
115. Find a vector whose magnitude is 2 and is parallel to  $\underline{i} + \underline{j} + \underline{k}$ .
116. Find  $\alpha$  so that the vectors  $2\underline{i} + \alpha\underline{j} + 5\underline{k}$  and  $3\underline{i} + \underline{j} + \alpha\underline{k}$  are perpendicular.
117. 129. Find  $\alpha$  so that  $\alpha\underline{i} + \underline{j}$ ,  $\underline{i} + \underline{j} + \alpha\underline{k}$ ,  $2\underline{i} + \underline{j} - 2\underline{k}$  are co-planar

## Long Questions

### 1. Chapter No. 1 (Functions and Limits)

- Evaluate  $\lim_{x \rightarrow 0} \frac{1 - \cos x}{\sin^2 x}$  17Grp I,
- Evaluate  $\lim_{x \rightarrow 0} \frac{\sin x}{x} = 1$